

Expanding Understandings of Embodied Mathematical Cognition in Students' Fraction Knowledge

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This study provides evidence that middle-grade students' symbolic fraction knowledge relates to grounded and embodied cognitive learning processes such as spatial ability and anxiety. These findings are consistent with previous findings^{1,2} while highlighting several novel associations: 1) Mental rotation and spatial visualization are specifically predictive of fraction knowledge scores; 2) Spatial anxiety may moderate the relationship between spatial ability and fraction knowledge scores; and 3) Fraction knowledge is not only grounded in processes operating at biological and cognitive timescales individually but components of these processes are interconnected. These findings may provide the foundations for future work exploring the mechanisms behind these associations.

THEORETICAL BACKGROUND

We draw on the Grounded and Embodied Learning Framework³, which describes the interconnected nature of learning across timescales including:

*biological

(affective states & memory)



seconds

to hours RATIONAL/ KNOWLEDGE-BASED

days to months SOCIOCULTURAL

*cognitive

+ 10⁸ years & beyond ORGANIZATIONAL

PARTICIPANTS:

- 4th year of a longitudinal study
- N = 89
- Female (38%), No answer (6%)
- 5th grade (62%), 8th Grade (38%)

PROCEDURE:

- Two 2-hour sessions to complete assessments (in-person or virtual)
- Interrupted due to COVID-19

MEASURES:

- Fraction Knowledge Assessment
- Woodcock-Johnson Tests III
- - Spatial Anxiety
 - Large Scale, Small Scale
 - Woodcock-Johnson Tests III - Math Fluency, Calculation - Spatial Reasoning Instrument
 - Visualization

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(spatial ability & number sense)



- Auditory Working Memory - Math Anxiety Rating Scale

- Mental Rotation, Orientation,



NGISSION

- Spatial ability, specifically spatial visualization and mental rotation skills, are significantly predictive of symbolic fraction knowledge and may be moderated by spatial anxiety.
- These associations may be indicative of how students ground fraction **knowledge** in a non-symbolic **ratio processing system**⁴ and evidence a link between mental rotation and SNARC effect magnitude⁵.
- Both biological and cognitive embodied processes^{3,6} were correlate with learning and thinking about fractions. Though many fraction knowledge researchers focus on one single variable, these correlations may indicate additional variables and relationships of interest in future work.

RESEARCH QUESTION

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How are mathematical learning and thinking about fractions rooted in body-based processes?

We used caluated Pearson's correlations to estimate magnitude and direction of the relationships between variables across embodied processes including:



REFERENCES

¹DeWolf, M., Bassock, M., & Holyoak, K. J. (2015). From rational numbers to algebra: Separable contributions of decimal magnitude and relational understanding of fractions. Journal of Experimental Child Psychology, 133, 72 - 84. of fractions. Frontiers in Psychology, 10, 596. ³Nathan, M. J. (2021). Foundataions of embodied learning: A paradigm for education. Routledge. ⁴Park, Y., & Matthews, P. G. (2021). Revisiting and refining the relations between nonsymbolic ratio processing and symbolic mathematics achievement. *Journal of Numerical Cognition*, 7, 328 - 350. ⁵Viarouge, A., Hubbard, E. M., & McCandliss, B. D. (2014). The cognitive mechanims of the SNARC effect: an individual differences approach. *PloS one*, 9, e95756. ⁶Newell, A. (1994). Unified theories of cognition. Harvard University Press.

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²Toomarian, E. Y., & Hubbard, E. M. (2019). Individual differences in implicit and explicit spatial processing